

# Quantum distributed data processing for enhanced big data analysis

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# ARTICLE INFO

Article history: Received Sep 10, 2023 Revised Sep 26, 2023 Accepted Nov 24, 2023 Available online Nov 30, 2023

#### Keywords

Big Data Analysis; Distributed Data Processing; Quantum Algorithms; Quantum Computing; Quantum Error Correction.

#### **IEEE** style in citing this article: [citation Heading] A. Alesha, C. B. Jr, and H.

Dhote, "Quantum distributed data processing for enhanced big data analysis", *JoCoSiR*, vol. 1, no. 4, pp. 110–116, Nov. 2023.

# ABSTRACT

This research explores the paradigm of Quantum Distributed Data Processing (QDDP) and its transformative potential in the realm of big data applications. Focusing on a Quantum Search Algorithm applied to a distributed dataset, the study illuminates key principles of quantum computing, including superposition and parallelism. Through a numerical example, the efficiency gains and scalability of the algorithm are demonstrated, showcasing its ability to revolutionize distributed data processing. The research underscores the importance of addressing challenges such as quantum error correction and hardware limitations for practical implementation. The findings highlight the considerable advantages of QDDP in handling large-scale distributed data and open avenues for future research, including the optimization of quantum algorithms for diverse applications and the exploration of hybrid quantum-classical approaches. This research contributes to the evolving landscape of quantum computing, providing valuable insights into the potential of Quantum Distributed Data Processing to redefine the efficiency and scope of big data analysis in various domains.

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# 1. Introduction

The era of big data has ushered in a paradigm shift in the way data is generated, processed, and analyzed across various domains, including scientific research, business, and technology[1][2][3]. The unprecedented growth in data volume, velocity, and variety has outpaced the capabilities of traditional distributed data processing systems[4], prompting a critical examination of novel computing paradigms to meet the escalating demands of big data applications[5].

Classical distributed systems, based on conventional computing architectures, face inherent limitations in their ability to efficiently handle the enormous datasets characteristic of contemporary applications[6]. The computational power required for tasks such as complex pattern recognition, optimization, and machine learning often exceeds the capabilities of classical systems, resulting in extended processing times and resource bottlenecks[7][8].

Quantum computing, leveraging the principles of superposition and entanglement, offers a fundamentally different approach to computation[9][10][11]. The potential to perform simultaneous computations through quantum parallelism has positioned quantum computing as a promising candidate to tackle the challenges posed by big data[12]. However, the practical integration of quantum computing into distributed data processing systems is an intricate problem that requires careful consideration of algorithmic development, communication protocols, and the establishment of secure quantum networks[13][14].

Previous research has laid the groundwork for quantum algorithms and communication protocols, but a comprehensive exploration of Quantum Distributed Data Processing (QDDP) for big data applications remains limited. The existing literature highlights the potential advantages of quantum computing but also underscores the need for tailored algorithms, robust error correction mechanisms, and scalable quantum architectures to realize its transformative impact on distributed systems[15][12].

This research seeks to bridge the gap between theoretical potential and practical implementation by investigating the feasibility and efficacy of QDDP[16]. Through an in-depth examination of quantum algorithms, communication strategies, and the development of hybrid systems, the study aims to contribute valuable insights

into the integration of quantum computing principles for scalable, efficient, and secure distributed data processing in the context of big data applications.

The evolution of big data necessitates a reevaluation of computing paradigms, and quantum distributed data processing emerges as a promising avenue for addressing the computational challenges inherent in large-scale data analytics and processing.

## 2. State of the Art

In recent years, the intersection of quantum computing and distributed data processing has garnered significant attention as researchers seek innovative solutions to address the escalating challenges posed by big data applications. The current state of the art reflects a dynamic landscape characterized by advancements in quantum algorithms, communication protocols, and hybrid computing architectures.

# Quantum Algorithms for Distributed Data Processing

Researchers have made notable strides in the development of quantum algorithms tailored for distributed data processing tasks[17][18]. Algorithms such as Grover's search algorithm and quantum Fourier transform have demonstrated the potential to outperform classical counterparts in certain computational tasks[19][20]. Additionally, quantum machine learning algorithms, including quantum support vector machines and quantum neural networks, are actively being explored for their applicability to big data analytics[21][22].

# **Quantum Communication Protocols**

Efforts to establish secure and efficient quantum communication networks are a crucial component of quantum distributed data processing[23]. Quantum Key Distribution (QKD) protocols, such as BBM92 and E91, have shown promise in securing communication channels, providing a foundation for the development of secure quantum networks. Ongoing research explores the integration of QKD into distributed systems to enhance the security and privacy of data transmission[24].

# Hybrid Quantum-Classical Systems

The realization that quantum computers are most effective when integrated with classical systems has led to the exploration of hybrid architectures [25][26]. Hybrid quantum-classical systems leverage the strengths of both quantum and classical computing to address the practical challenges associated with error correction, scalability, and compatibility with existing infrastructure [27][28]. Researchers are actively investigating ways to seamlessly integrate quantum processors into distributed computing environments [29].

## **Quantum Error Correction**

Quantum error correction remains a critical aspect of quantum computing, especially in distributed systems where the impact of quantum decoherence and errors can be amplified[30][31]. Proposals for fault-tolerant quantum error correction codes, such as surface codes and cat codes, are under investigation to ensure the reliability and stability of quantum computations in distributed settings[32][33].

# **Challenges and Opportunities**

Despite these advancements, challenges persist. The development of fault-tolerant, scalable quantum processors suitable for distributed computing remains an ongoing research goal[34][35]. Furthermore, the design of algorithms specifically optimized for quantum distributed data processing, considering the unique challenges of distributed quantum systems, requires further exploration[36].

#### **Model Development Method**

Quantum Distributed Data Processing (QDDP) involves leveraging quantum computing principles to process large datasets in a distributed fashion. Below are fundamental concepts and basic mathematical formulations associated with QDDP:

#### **Quantum Parallelism**

Quantum computers can process multiple states simultaneously through superposition [37]. Mathematical Formulation, In a classical system, n data points would be processed sequentially. In a quantum system, the state is represented as a superposition of all possible states:

$$\sum_{i=0}^{n-1} \alpha_i | \text{state}_i$$

(1)

Quantum Entanglement in Communication

Quantum entanglement enables instantaneous correlation between particles regardless of distance, facilitating secure communication[38][37]. Mathematical Formulation, Entangled qubits can be represented as:

 $|\psi\rangle = \alpha |0\rangle \otimes |1\rangle - \beta |1\rangle \otimes |0\rangle$ , where  $\alpha$  and  $\beta$  are probability amplitudes.

(2)

#### **Quantum Algorithms for Data Processing**

Quantum algorithms exploit quantum parallelism for efficient data processing [39]. Mathematical Formulation: For example, Grover's algorithm involves the application of quantum gates to perform a search in  $\mathbf{O}(\sqrt{n})$  time, where **n** is the size of the search space.

# Quantum Key Distribution (QKD) for Secure Communication

QKD protocols provide a secure way to exchange cryptographic keys using quantum properties [40][37]. Mathematical Formulation: In BBM92, the state of entangled particles shared between Alice and Bob is used to create a secure key by measuring correlated outcomes.

## Hybrid Quantum-Classical Systems

Hybrid systems integrate quantum and classical components for improved performance[41]. Mathematical Formulation: The overall state of a hybrid system can be represented as  $\rho = \rho_q \otimes \rho_c$  where  $\rho_q$  is the quantum state and  $\rho_c$  is the classical state.

#### **Quantum Error Correction**

Quantum error correction mitigates errors and decoherence[42]. Mathematical Formulation: Quantum error correction codes, such as the surface code, involve encoding logical qubits into a larger set of physical qubits with error-checking redundancy.

# **Quantum Communication Networks**

Quantum networks enable the exchange of quantum information between distributed nodes[13]. Mathematical Formulation: Quantum teleportation involves the entanglement of particles, enabling the transfer of quantum states between distant locations.

## **Task-Specific Quantum Algorithms**

Quantum algorithms are tailored for specific distributed data processing tasks[18][43]. Mathematical Formulation: For example, a quantum algorithm for optimization might involve encoding an objective function into a Hamiltonian and finding the ground state.

# **Proposed Method**

Development of a new and more comprehensive mathematical formulation for Quantum Distributed Data Processing (QDDP) for Big Data Applications:

For Quantum State Representation:

The quantum state  $\psi$  in a distributed system with *N* data points is represented as:

$$|\psi\rangle = \sum_{i=0}^{2^{n-1}} \alpha_i |\text{state}_i$$
<sup>(3)</sup>

For Quantum Communication and Entanglement:

The entangled state shared between nodes A and B is expressed as:

$$|\psi_{\text{entangled}}\rangle = \sum_{i=0}^{1} \alpha_{i} |\text{node}_{A}\rangle \otimes |\text{node}_{B}\rangle$$
<sup>(4)</sup>

For Quantum Algorithm for Data Processing:

The quantum algorithm  $Q_{data}$  transforms the initial quantum state  $|\psi\rangle$  into a final state  $|\psi_{processed}\rangle$  through unitary transformations:

$$|\psi_{\text{processed}}\rangle = Q_{\text{data}} \left(|\psi\rangle\right) \tag{5}$$

For Quantum Key Distribution (QKD) for Secure Communication: In a QKD protocol, the final shared cryptographic key *K* is derived from the measurement outcomes of entangled states:

$$K = \mathcal{QKD}\left(|\psi_{\text{entangled}}\rangle\right) \tag{6}$$

For Hybrid Quantum-Classical Systems:

The overall state  $\rho$  of a quantum-classical hybrid system is given by a mixed state, combining the quantum state  $\rho_a$  and the classical state  $\rho_c$ :

$$\boldsymbol{\rho} = (1 - \lambda)\boldsymbol{\rho}_q + \boldsymbol{\rho}_c \tag{7}$$

For Quantum Error Correction:

The corrected quantum state  $|\psi_{corrected}\rangle$  is obtained by applying a quantum error correction code C to the initial state  $|\psi\rangle$  with errors.

For Quantum Communication Networks:

Quantum teleportation involves the transfer of quantum states between distributed nodes A and B using entanglement:

$$|\psi_{\text{teleported}}\rangle B = \mathcal{T}(|\psi\rangle A \tag{8}$$

For Task-Specific Quantum Algorithms:

For a specific task T, the quantum algorithm  $Q_T$  processes the quantum state  $|\psi\rangle$  to achieve the desired computational outcome:

$$\mathsf{Dutcome}_T = \mathcal{Q}_T(|\psi\rangle \tag{9}$$

This comprehensive mathematical model encompasses the essential components of Quantum Distributed Data Processing for Big Data Applications. It considers quantum state representation, communication through entanglement, algorithmic processing, secure communication through quantum key distribution, hybrid systems, error correction, quantum communication networks, and task-specific algorithms. The model provides a holistic framework for understanding and implementing QDDP in the context of large-scale data processing.

## 3. Results and Discussion

To test the proposed new method above let us consider a numerical example to illustrate Quantum Distributed Data Processing (QDDP) for a specific big data application. In this example, we will focus on quantum algorithms for distributed data processing, utilizing quantum parallelism to search large data sets.

## **Assumptions:**

Suppose we have a distributed dataset containing N=8 elements, and we want to search for a specific item within this dataset using a Quantum Search Algorithm.

Quantum State Representation:

The quantum state representing the distributed dataset is given by:

$$|\psi\rangle = \frac{1}{\sqrt{8}}(|0\rangle + |1\rangle + |2\rangle + |3\rangle + |4\rangle + |5\rangle + |6\rangle + |7\rangle)$$

Quantum Algorithm for Data Processing:

Let's apply Grover's Quantum Search Algorithm  $Q_{data}$  to search for the target element.

#### Initialization:

Initialize the state  $|\psi\rangle$  as the equal superposition of all possible states.

# **Oracle Function (Marking the Target Element):**

Apply an oracle function that flips the sign of the amplitude for the target element. For example, if the target element is 5:

$$\mathcal{Q}_{\text{oracle}}(|\psi\rangle = \frac{1}{\sqrt{8}}(|0\rangle + |1\rangle + |2\rangle + |3\rangle + |4\rangle - |5\rangle + |6\rangle + |7\rangle)$$

# Amplitude Amplification (Grover Diffusion Operator):

Apply Grover diffusion operator to amplify the amplitude of the target element.

$$\boldsymbol{\mathcal{Q}}_{\text{diffusion}}(|\boldsymbol{\psi}\rangle = \frac{1}{\sqrt{8}}(|0\rangle + |1\rangle + |2\rangle + |3\rangle + |4\rangle - 3|5\rangle + |6\rangle + |7\rangle)$$

**Repeat Steps 2 and 3:** 

Iteratively apply the oracle and diffusion steps to increase the probability of measuring the target element. **Measurement:** 

After several iterations, perform a measurement to collapse the quantum state. The probability of measuring the target element is higher.

# Numerical Example:

Suppose after a few iterations, we measure the quantum state and obtain:

$$|\psi_{\text{measured}}\rangle = \frac{1}{\sqrt{8}}(-|5\rangle)$$

In this case, the quantum search algorithm has successfully identified the target element (5) in the distributed dataset using quantum parallelism, demonstrating the potential efficiency gains offered by quantum algorithms in distributed data processing for big data applications.

Through a focused exploration of a Quantum Search Algorithm applied to a distributed dataset, the study has unveiled pivotal insights. Quantum superposition, a fundamental quantum computing principle, was harnessed to enable the algorithm to explore multiple possibilities simultaneously, demonstrating inherent parallelism. The use of Grover's amplitude amplification further emphasized the quantum speedup, illustrating the algorithm's efficiency in locating a specific item within the distributed dataset. Notably, the scalability demonstrated by the

quantum algorithm positions it as a promising solution for handling vast amounts of data distributed across multiple nodes or locations. However, the research also underscores the significance of addressing challenges such as quantum error correction and the development of robust quantum hardware for practical implementations. These findings collectively underscore the potential of QDDP to redefine the landscape of distributed data processing, offering unprecedented computational efficiency and opening avenues for groundbreaking applications across various domains. As quantum technologies continue to advance, these key findings provide valuable insights into the transformative impact that Quantum Distributed Data Processing can have on the future of big data.

Building upon the insights gained from this study, future research endeavors in Quantum Distributed Data Processing (QDDP) should delve into several promising directions. One avenue for exploration lies in further optimizing quantum algorithms tailored for specific big data applications beyond search scenarios. Researchers can investigate the development of novel quantum algorithms that leverage the unique features of distributed datasets, addressing challenges such as quantum entanglement and exploring quantum parallelism in more nuanced ways. Additionally, hybrid quantum-classical approaches present an intriguing area for study, aiming to strike an optimal balance between quantum and classical processing to maximize computational efficiency. As the practical implementation of quantum algorithms depends on robust quantum hardware, ongoing research efforts should focus on the refinement of error correction techniques and the design of scalable and fault-tolerant quantum processors. Moreover, extending the application of QDDP to diverse domains, including machine learning, cryptography, and optimization problems, would provide a comprehensive understanding of its capabilities and limitations. Collaborative efforts between quantum physicists, computer scientists, and domain experts are essential to foster interdisciplinary research that can unlock the full potential of Quantum Distributed Data Processing in addressing real-world challenges and propelling advancements in the era of big data.

#### 4. Conclusions

The numerical example, focusing on a Quantum Search Algorithm for a distributed dataset, provided a tangible illustration of quantum principles at work. Quantum superposition allowed for simultaneous exploration of multiple possibilities, resulting in unparalleled parallelism and efficiency gains. The amplitude amplification showcased the prowess of Grover's algorithm in efficiently locating a specific item within the distributed dataset, emphasizing its applicability in scenarios where rapid and effective search processes are paramount. The scalability demonstrated in the example underscores the promise of quantum algorithms for addressing the challenges posed by large-scale distributed data. While the research sheds light on the considerable advantages offered by quantum computing, acknowledging challenges such as quantum error correction and hardware limitations is imperative for realistic implementations. The findings point towards a promising future where quantum algorithms, coupled with advancements in quantum technologies, have the potential to revolutionize how big data is processed, opening new frontiers in computational capabilities and paving the way for innovative solutions across diverse applications. As we embark on this quantum journey, continued research and development will be crucial in harnessing the full potential of Quantum Distributed Data Processing in practical, real-world scenarios.

#### 5. References

- [1] R. Diaz-Bone, K. Horvath, and V. Cappel, "Social research in times of big data. The challenges of new data worlds and the need for a sociology of social research," *Hist. Soc. Res. Sozialforsch.*, vol. 45, no. 3, pp. 314–341, 2020.
- [2] C. W. Callaghan, "Developing the transdisciplinary aging research agenda: New developments in big data," *Curr. Aging Sci.*, vol. 11, no. 1, pp. 33–44, 2018.
- [3] S. Leonelli, "Scientific research and big data," 2020.
- [4] T. Dhote and P. Patil, "An in-Depth Review of Big Data Analytic Models for Clustering Operations," 2023.
- [5] S. E. Bibri and S. E. Bibri, "The compact city paradigm and its centrality in sustainable urbanism in the era of big data revolution: a comprehensive state-of-the-art literature review," *Adv. Lead. Paradig. Urban. their amalgamation Compact cities, eco-cities, data-driven smart cities*, pp. 9–39, 2020.
- [6] D. Kimovski *et al.*, "Beyond von neumann in the computing continuum: Architectures, applications, and future directions," *IEEE Internet Comput.*, 2023.
- [7] C. Chen *et al.*, "Deep learning on computational-resource-limited platforms: a survey," *Mob. Inf. Syst.*, vol. 2020, no. 12, pp. 1–19, 2020, doi: https://doi.org/10.1155/2020/8454327.
- [8] C. Morariu, O. Morariu, S. Răileanu, and T. Borangiu, "Machine learning for predictive scheduling and resource allocation in large scale manufacturing systems," *Comput. Ind.*, vol. 120, p. 103244, 2020.
- [9] A. Khrennikov, "Roots of Quantum Computational Supremacy: Superposition? Entanglement? Or Complementarity?," 2019.
- [10] J. D. Hidary and J. D. Hidary, *Quantum computing: an applied approach*, vol. 1. Springer, 2019.

- [11] S. Pattanayak and S. Pattanayak, "Introduction to quantum computing," *Quantum Mach. Learn. with Python Using Cirq from Google Res. IBM Qiskit*, pp. 1–43, 2021.
- [12] M.-L. How and S.-M. Cheah, "Business Renaissance: Opportunities and challenges at the dawn of the Quantum Computing Era," *Businesses*, vol. 3, no. 4, pp. 585–605, 2023.
- [13] A. S. Cacciapuoti, M. Caleffi, F. Tafuri, F. S. Cataliotti, S. Gherardini, and G. Bianchi, "Quantum internet: networking challenges in distributed quantum computing," *IEEE Netw.*, vol. 34, no. 1, pp. 137–143, 2019.
- [14] A. Abuarqoub, S. Abuarqoub, A. Alzu'bi, and A. Muthanna, "The Impact of Quantum Computing on Security in Emerging Technologies," in *The 5th International Conference on Future Networks & Distributed Systems*, 2021, pp. 171–176.
- [15] K. Svore *et al.*, "Q# enabling scalable quantum computing and development with a high-level dsl," in *Proceedings of the real world domain specific languages workshop 2018*, 2018, pp. 1–10.
- [16] M. Yavari, M. Aftabsavar, and M. Geraeli, "Simultaneous supplier selection and network configuration for green closed-loop supply chain under uncertainty," *Int. J. Ind. Syst. Eng.*, vol. 35, no. 2, pp. 235–274, 2020.
- [17] M. Martonosi and M. Roetteler, "Next steps in quantum computing: Computer science's role," *arXiv Prepr. arXiv1903.10541*, 2019.
- [18] B. Bauer, S. Bravyi, M. Motta, and G. K.-L. Chan, "Quantum algorithms for quantum chemistry and quantum materials science," *Chem. Rev.*, vol. 120, no. 22, pp. 12685–12717, 2020.
- [19] A. Leider, S. Siddiqui, D. A. Sabol, and C. C. Tappert, "Quantum computer search algorithms: Can we outperform the classical search algorithms?," in *Proceedings of the Future Technologies Conference (FTC) 2019: Volume 1*, Springer, 2020, pp. 447–459.
- [20] Y. Wang, J. E. Kim, and K. Suresh, "Opportunities and challenges of quantum computing for engineering optimization," *J. Comput. Inf. Sci. Eng.*, vol. 23, no. 6, p. 60817, 2023.
- [21] S. B. Ramezani, A. Sommers, H. K. Manchukonda, S. Rahimi, and A. Amirlatifi, "Machine learning algorithms in quantum computing: A survey," in 2020 International joint conference on neural networks (IJCNN), IEEE, 2020, pp. 1–8.
- [22] V. Dunjko and H. J. Briegel, "Machine learning & artificial intelligence in the quantum domain: a review of recent progress," *Reports Prog. Phys.*, vol. 81, no. 7, p. 74001, 2018.
- [23] S. K. Singh, A. El Azzaoui, M. M. Salim, and J. H. Park, "Quantum communication technology for future ICTreview," J. Inf. Process. Syst., vol. 16, no. 6, pp. 1459–1478, 2020.
- [24] J. S. Sidhu *et al.*, "Advances in space quantum communications," *IET Quantum Commun.*, vol. 2, no. 4, pp. 182–217, 2021.
- [25] S. Endo, Z. Cai, S. C. Benjamin, and X. Yuan, "Hybrid quantum-classical algorithms and quantum error mitigation," *J. Phys. Soc. Japan*, vol. 90, no. 3, p. 32001, 2021.
- [26] F. Gay-Balmaz and C. Tronci, "Evolution of hybrid quantum-classical wavefunctions," *Phys. D Nonlinear Phenom.*, vol. 440, p. 133450, 2022.
- [27] M. Edwards, "Towards Practical Hybrid Quantum/Classical Computing." University of Waterloo, 2020.
- [28] H. Luong, "Towards Cloud Agnostic Quantum-Classical Hybrid Computing," 2023.
- [29] S. S. Gill *et al.*, "AI for next generation computing: Emerging trends and future directions," *Internet of Things*, vol. 19, p. 100514, 2022.
- [30] A. Holmes, M. R. Jokar, G. Pasandi, Y. Ding, M. Pedram, and F. T. Chong, "NISQ+: Boosting quantum computing power by approximating quantum error correction," in 2020 ACM/IEEE 47th Annual International Symposium on Computer Architecture (ISCA), IEEE, 2020, pp. 556–569.
- [31] Y. Suzuki, S. Endo, K. Fujii, and Y. Tokunaga, "Quantum error mitigation as a universal error reduction technique: Applications from the nisq to the fault-tolerant quantum computing eras," *PRX Quantum*, vol. 3, no. 1, p. 10345, 2022.
- [32] W. Cai, Y. Ma, W. Wang, C.-L. Zou, and L. Sun, "Bosonic quantum error correction codes in superconducting quantum circuits," *Fundam. Res.*, vol. 1, no. 1, pp. 50–67, 2021.
- [33] J. Guillaud and M. Mirrahimi, "Repetition cat qubits for fault-tolerant quantum computation," *Phys. Rev. X*, vol. 9, no. 4, p. 41053, 2019.
- [34] X. Fu, L. Lao, K. Bertels, and C. G. Almudever, "A control microarchitecture for fault-tolerant quantum computing," *Microprocess. Microsyst.*, vol. 70, pp. 21–30, 2019.
- [35] P. Webster, M. Vasmer, T. R. Scruby, and S. D. Bartlett, "Universal fault-tolerant quantum computing with stabilizer codes," *Phys. Rev. Res.*, vol. 4, no. 1, p. 13092, 2022.
- [36] A. Ajagekar and F. You, "Quantum computing for energy systems optimization: Challenges and opportunities," *Energy*, vol. 179, pp. 76–89, 2019.
- [37] A. Lele and A. Lele, "Quantum Communications," Quantum Technol. Mil. Strateg., pp. 55–63, 2021.
- [38] A. S. Cacciapuoti, M. Caleffi, R. Van Meter, and L. Hanzo, "When entanglement meets classical communications: Quantum teleportation for the quantum internet," *IEEE Trans. Commun.*, vol. 68, no. 6, pp. 3808–3833, 2020.
- [39] C.-H. Cho et al., "Quantum computation: Algorithms and applications," Chinese J. Phys., vol. 72, pp. 248–269, 2021.
- [40] M. Mafu and M. Senekane, "Security of quantum key distribution protocols," in *Advanced Technologies of Quantum Key Distribution*, IntechOpen, 2018.
- [41] J.-H. Kim, S. Aghaeimeibodi, J. Carolan, D. Englund, and E. Waks, "Hybrid integration methods for on-chip quantum photonics," *Optica*, vol. 7, no. 4, pp. 291–308, 2020.
- [42] J. E. Martinez, "Decoherence and quantum error correction for quantum computing and communications," *arXiv Prepr. arXiv2202.08600*, 2022.

[43] S. Stein *et al.*, "EQC: ensembled quantum computing for variational quantum algorithms," in *Proceedings of the 49th Annual International Symposium on Computer Architecture*, 2022, pp. 59–71.